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# Some Peculiarities of Behavior of the System "Rigid Mooring Retaining Wall — Soil Media"

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**Abstract:** The proposed model of the system "rigid mooring retaining wall — soil media" allows considering kinematics factors of the structure and to use when designing and calculating variable values of main system parameters, corresponding to its current deformed and stressed states. The main results of the model development and its applied aspects are presented in the paper. Soil pressure dependencies (displacement–pressure) are studied, including peculiarities related to the state at rest.

Key words: Mooring retaining wall, soil pressure, stressed-deformed state, state at test.

### 1. Introduction

Soil pressure at rest is one of the basic characteristics used in the analysis stressed-deformed state of the system "retaining wall — soil media". The role of this parameter is especially significant when considering rigid constructions, where displacements or deformations are insufficient for the realization of active or passive pressure. It is known that the stressed state of the soil, even at a motionless wall, can transform depending on the direction and value of the external loading exerted upon the retaining wall. As an illustration of the mentioned, diagrams from "Maritime recommendations" [1] (Fig. 1) can serve. Here, the dependencies of the factor of soil lateral pressure on retaining wall deformations (angles of rotation about the bottom end) are reflected.

From the dependencies presented in Fig. 1, it is visible that pressure at rest is defined not by a point on the axis of factors of soil lateral pressure, but a piece on this axis. The curve describing active pressure begins from the bottom border of this piece, and the curve describing reactive soil pressure on a wall starts from its top border. It is necessary to note that the size

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of this piece is not a constant and depends on the physical characteristics of the soil. For a loose soil, the zone of pressure at rest on an axis of factors of lateral pressure is much more than the zone corresponding to a dense soil.

As to Eurocode 7 [2], it supposes the use of certain "intermediate" values of soil lateral pressure when displacements of a retaining wall are insufficient for mobilization of ultimate values.

Some European codes recommend calculating soil pressure at rest as active pressure using a conditional angle of internal friction of the soil. It means that above mentioned piece of a zone of rest on an axis of factors of soil lateral pressure on Fig. 1 should be shown as a point conterminous to the bottom end of this piece.

### 2. Soil Media — Retaining Wall Interaction Model

This model is based on the concept of the so-called "threshold of gravitation" [3-7]. It is caused by an inequality of values of soil pressure at rest, corresponding to potential displacement of a retaining wall away from a soil (preliminary stage of active pressure) and towards a soil (preliminary stage of reactive pressure).

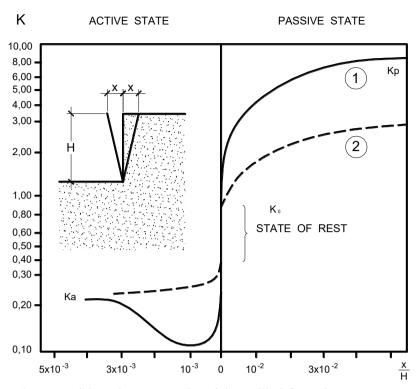


Fig. 1 Dependences between soil lateral pressure and retaining wall's deformations.

The physical sense of this parameter may be explained as follows. The soil active wedge is formed almost simultaneously with the beginning of the wall's displacement because of the action of friction forces that are promoted by the gravity of the soil. At the wall's displacement towards the soil, its gravity interferes with the displacement. So, only because of overcoming this factor (which is offered to assess numerically by the value of "threshold of gravitation"), the action of friction forces in a soil results in the formation of a reactive prism.

As pressure at rest is the important starting point at definition of stressed — deformed state of the system "retaining wall — soil media" in many geo-engineering important designs (deep-water quay walls, walls of dry docks, tunnels, etc.), perfection of methods of definition of this base parameter essentially influences both reliability of a construction, and on its technical and economic parameters.

Based on the known experimental research (for example, Lubenov, 1962; Yakovlev, 1968, 1987 [8-11]), it is possible to assume (similarly to formation

of sliding surfaces corresponding to active or reactive wedges at the wall's displacement), that some conditional soil wedge corresponds to the soil pressure upon the motionless wall (wedge at rest). As discovered, the sizes of this wedge exceed the dimensions of an active wedge (the last corresponds to the formation of active soil pressure and critical wall's displacement away from the ground).

It is logical to assume that in the case of an opposite direction of construction displacement (towards a soil) dimensions of the wedge at rest will increase, approaching a limit to the sizes of the wedge corresponding to passive pressure. At an initial stage of this process (at the exerting of external loading, but before the beginning of wall displacement towards the soil), there is a rearrangement of the stressed state of the soil interacting with a retaining wall. Thus, the conditional active wedge (stipulated by active soil pressure behind the wall) is transformed to a conditional reactive wedge because an external lateral loading on a wall compensates initial active soil pressure. When external lateral loading on a wall

reaches the value capable of causing displacement of the construction towards the soil, the conditional reactive wedge is transformed into a real one. At the moment when reactive pressure reaches the value of passive pressure (at the ultimate state), this reactive wedge can be transferred to the soil bulging wedge. The considered process is characterized not only by an increase in the sizes of the reactive wedge, but also by a change of its geometry because the conditional angle of internal friction (on which geometrical parameters of reactive edge depend) increases (in a limit) up to the value of the angle of internal friction.

Let's name the pressure corresponding to the initial stage of formation of soil stressed state regarding potential wall displacement towards the soil (for example, during the initial moment of the exerting on the retaining wall of external lateral loading) as pre-reactive pressure. Similarly, the pressure corresponding to the initial stage of formation of soil stressed state regarding potential wall displacement

away from the soil will be named as pre-active pressure.

Hence (regarding above mentioned circumstances), pre-reactive pressure will be more than the pre-active one. As pre-reactive pressure (considering its formation and realization) is similar to reactive one (in the ultimate state, to passive pressure), it is expedient to apply formulas related to the calculation of reactive pressure, but using values of an angle of internal friction of the soil, corresponding to its current stressed — deformed state.

Thus, the soil stressed state on contact to a motionless retaining wall in researched model is described not by a point  $e_0$  on an axis of pressure (as in the traditional approach — Fig. 2a), but by a piece limited from below to value  $e_{oa}$  (the pressure at rest determined on dependences for active pressure), and from above — value  $e_{op}$  (the pressure at rest determined on dependences for reactive pressure) (Fig. 2b).

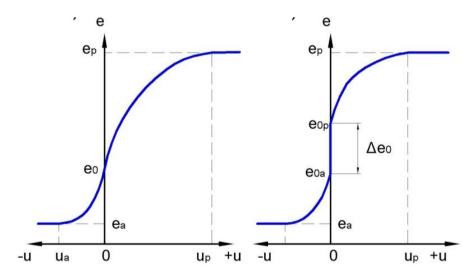


Fig. 2 Illustrations of the proposed approach: dependence of soil lateral pressure on a retaining wall's displacements.

Thus, the entered concept of "a threshold of gravitation" can be described by the expression

$$_{\Delta}e_{o}=e_{op}$$
 -  $e_{oa}$ ,

where  $e_{op}$  and  $e_{oa}$  — soil lateral pressure at rest, determined accordingly under formulas for reactive and active pressures.

For quantitative assessment of the considered process, the relative parameter can serve (we'll name it as a factor of the transformation). A factor of the transformation is equal to the ratio of the considered values of soil lateral pressure at rest:

$$K_t = e_{op} / e_{oa}$$
.

The possible effect of the suggested approach is illustrated by the diagram in Fig. 3, where qualitative dependences "reactive pressure-displacement" for the retaining wall perceiving external loading and moving

towards the soil are submitted. Curve 1 corresponds to the pressure at rest, determined under formulas of active pressure, and curve 2 — to the pressure at rest, determined under formulas of reactive pressure.

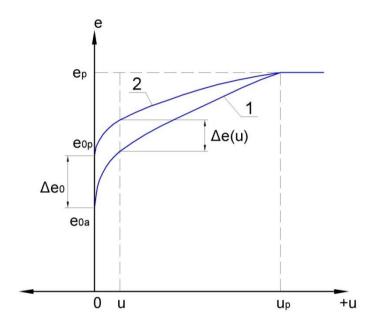


Fig. 3 Dependences "reactive pressure-displacements".

At a motionless wall, the difference between pressure at rest in case of 1 (pressure  $e_{oa}$ ) and in case of 2 (pressure  $e_{op}$ ) makes "a threshold of gravitation"  $\Delta e_o$ . At the formation and increasing of displacements of points on a contact surface of a wall towards a soil, the reactive pressure changes in the considered cases according to curves 1 or 2.

Thus, the difference  $\Delta e$  (u) of reactive pressure values, corresponding to some moving "u" and caused by various initial soil stressed states (pressure of rest  $e_{oa}$  and  $e_{op}$ ) can be rather significant. As calculations show, at a motionless contact surface of a retaining wall, and at values "u" in a vicinity of "zero" displacements, the difference between values of initial pressures  $e_{oa}$  and  $e_{op}$  can reach several hundred percent and essentially influence operating conditions of the whole structure. Accordingly, the value of soil lateral pressure at rest increases at the moment

just before the beginning of displacement of a retaining wall towards a soil because of the application of external lateral loading to a construction.

To calculate the values of pressure at rest, it is necessary to use the corresponding values of soil internal friction angle  $\varphi_o$ . In the work of Klein (1977) [12], the following dependence was offered:

$$\varphi_0 = arcsin(1-K_0/1+K_0)$$

where K<sub>o</sub> is a factor of soil lateral pressure at rest.

It would be methodologically correct to link a conditional angle of soil internal friction with its real values. With this purpose Jaki formula can be applied for granulated soils:

$$K_o = 1$$
-sin  $\varphi$ 

Given the previous dependence, the formula connecting the conditional and real angles of soil internal friction can be obtained as:

$$\varphi_0 = arcsin \left[ sin\varphi/(2-sin\varphi) \right]$$

## 3. Some Results of Pressure at Rest Numerical Modeling

Below are some results of the qualitative and quantitative analysis of the data received by numerical modeling of the interaction of elements of the system "a retaining wall — the soil media" are considered. Based on the developed model influence of its base initial data (an angle of internal friction  $\phi$  and an angle of friction  $\delta$  of the soil on the contact surface of a wall) on the parameters of soil lateral pressure at rest has been studied.

For simplification of the analysis, the retaining wall of gravitational type with a vertical rear contact side and a horizontal unloaded free surface of filling behind of the wall was considered regarding the following intervals of angles  $\varphi$  and  $\delta$ :

- $\varphi = 22^{\circ}, 24^{\circ}, 26^{\circ}, 28^{\circ}, 30^{\circ}, 32^{\circ};$
- $\delta = 0$ ; 0.25 $\phi$ ; 0.5 $\phi$ ; 0.75 $\phi$ ;  $\phi$ .

The resulting lateral pressure of soil upon a construction can be calculated from a known expression:

$$E = 0.5 \gamma h^2 K$$
,

Table 1 Some results of pressure at rest numerical modeling.

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	flat surfaces of sliding		curvilinear surfaces of sliding	
	influence of an angle of internal friction φ (values interval 22 <sup>0</sup> -32 <sup>0</sup> )			
	no contact friction $(\delta = 0)$	full contact friction $(\delta = \varphi)$	no contact friction $(\delta = 0)$	full contact friction ( $\delta$ = $\varphi$ )
Increase of factor of soil lateral pressure	1,10 - 1,61	1,81 - 3,30	1,10 - 1,61	1,71 - 2,91
Increase of factor of transformation	2,80 - 4,36	4,45 - 8,93	2,80 - 4,36	4,10 - 7,66
	influence of an angle of contact friction $\delta$ (values interval $0-\phi)$			
	$\varphi = 24^{\circ}$ - $32^{\circ}$		φ = 24°- 32°	
Increase of the threshold $\Delta e$	1.68 – 2.05		1.59 – 1.81	
Increase of the factor of transformation	1.59 - 2.047		1.46 – 1.76	

### 4. Conclusions

Consideration of such concepts as lateral pressure at rest allows taking into account the potential direction of displacement and deformations of a construction.

For an estimation of quantitative distinction

where  $\gamma$  – unit weight of a soil; h - height of a vertical contact side of a retaining wall; K - factor of lateral pressure of a soil.

It is convenient to present the soil lateral pressure caused by its weight in the dimensionless form:

$$e = E/(0.5 \gamma h^2),$$

where: e - the dimensionless force of lateral pressure of the ground, numerically equal to the factor of corresponding lateral pressure (active, passive, or at rest).

The numerical analysis was executed for both flat and curvilinear surfaces of soil sliding.

Formulas for calculating soil lateral pressure for the considered wall can be obtained from known, more general dependencies [13, 33].

Some results of the numerical analysis of soil lateral pressure at rest on a retaining wall are presented in Table 2.1. The basic qualitative conclusion from Table 2.1 is that with the increase of the value of  $\phi$  and  $\delta$ , the value of "a threshold of gravitation" and, accordingly, a factor of transformation, also increases. In Fig. 4 and 5 some samples of calculated dependencies are presented.

between "pre-active" and "pre-reactive" soil lateral pressure at rest, such parameters as "a threshold of gravitation" and factor of transformation are proposed and practically implemented in numerical analysis of retaining walls.

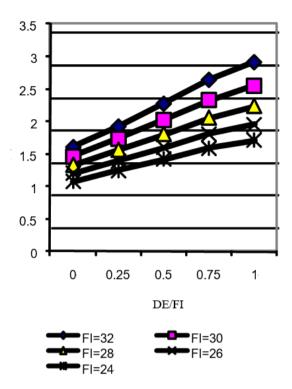


Fig. 4 Dependence between "threshold of gravitation" and the angle of soil contact friction (curvilinear surfaces of sliding).

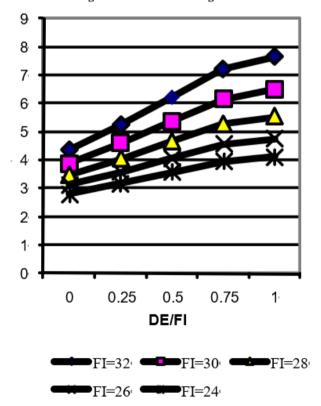


Fig. 5 Dependence between the factor of transformation and the angle of soil contact friction (curvilinear surfaces of sliding).

As "pre-active" soil lateral pressure at rest can exceed "pre-reactive" pressure in times (in an interval from three up to eight times depending on the soil properties), the account of the proposed parameters can increase essentially accuracy of designing and calculation of retaining walls and so to affect reliability and technical and economic parameters of constructions.

It is determined that an increase of both angles  $\phi$  and  $\delta$  is accompanied by an increase in both the "threshold of gravitation" and the factor of transformation.

As is known, values of active pressure, calculated both for flat and curvilinear surfaces of sliding, differ insignificantly, but values of reactive (passive) pressure turn out to be more exact (i.e., corresponding to the data of tests) in the case of use of curvilinear surfaces of sliding. In this connection, it may be recommended also to apply the formulas corresponding to curvilinear surfaces of sliding while determining soil pressure at rest and related parameters: "a threshold of gravitation" and factor of transformation.

### References

- [1] ROM 0.2-90, Actions in the design of maritime and harbor works, Maritime Works Recommendations, Ministerio de Obras Publicas y transportes, Madrid (1990).
- [2] Eurocode 7, Part 1. Geotechnical Design, General Rules. CEN – European Committee for Standardization, 1993.
- [3] Doubrovsky, M., & Poizner, M. (2016). *Innovative Development of Coastal, Port and Marine Engineering:*

- Structures, Technologies and Design, Lambert Academic Publishing, p. 136.
- [4] Doubrovsky, M. (2006). Determination of soil lateral pressure regarding displacements of retaining wall, in: *Proceedings of the XIII-th Danube-European Conference on Geotechnical Engineering*, Ljubljana.
- [5] Doubrovsky, M. et al. (2005). Assessment of soil lateral pressure depending on retaining wall displacements, in: Geotechnology in Harmony with the Global Environment: Proceedings of the 16th International Conference on Soil Mechanics and Geotechnical Engineering, Osaka, Japan, pp. 889-893.
- [6] Doubrovsky, M. et al. (2003). Influence of potential soil deformations on soil pressure at rest upon retaining wall: Geotechnical problems with man-made and man-influenced grounds, in: Proceedings of the XIIIth European Conference on Soil Mechanics and Geotechnical Engineering, Prague, Czech Republic, Vol. 2, pp. 521-526.
- [7] Doubrovsky, M. (1994). Determination of lateral soil pressure against a retaining wall with allowance for the structure's kinematics, *Soil Mech Found Eng.*, 31: 46-51.
- [8] Bugaev, V. T., Doubrovsky, M. P., Yakovlev, P. I., & Shtefan, A. V. (2001). Design of Dry Docks and Their Interaction With the Soil, Moscow: NEDRA.
- [9] Lubenov, R. V., & Yakovlev, P. I. (1962). Study of soil pressure on a motionless wall, *Hydraulic Engineering* — *Moscow: Marine Transport*, 2: 79-87.
- [10] Yakovlev, P. I., & Lubenov, R. V. (1968). Some new results of experimental research of soil pressure upon rigid walls, *Hydraulic Engineering Construction*, 7: 43-46.
- [11] Yakovlev, P. I. (1987). About some results of experimental study of the interaction of hydraulic engineering structures with a soil, *Hydraulic Engineering Constructions: Vladivostok*, 22-34.
- [12] Klein, G. K. (1977). Structural Mechanics of Non-cohesive Media, Moscow: STROYIZDAT.
- [13] Yakovlev, P. I. (1986). Stability of water-development works in transportation, *Transport*, Moscow.