

# Electronic Structure Investigation of 12442 Iron-Based Superconductors Based on Block-Layer Model

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**Abstract:** Superconducting transition temperature ( $T_c$ ), as a crucial parameter, exploring its relationship with various macroscopic and microscopic factors helps to understand the mechanism of high-temperature superconductivity from multiple perspectives, aiding in a multidimensional comprehension of high-temperature superconductivity mechanisms. Drawing inspiration from the block-layer structure models of cuprate superconductors, we computationally investigated the interlayer interaction energies in the 12442-type iron-based superconducting materials  $AkCa_2Fe_4As_4F_2$  ( $Ak = K, Rb, Cs$ ) systems based on the block-layer model and explored their relationship with  $T_c$ . We observed that an increase in interlayer combinative energy leads to a decrease in  $T_c$ , while conversely, a decrease in interlayer combination energy results in an increase in  $T_c$ . Further, we found that the contribution of the Fe 3d band structure, especially the  $3d_{z^2}$  orbital, to charge transfer is significant.

**Key words:** Block-layer structural mode, iron-based superconductor, combinative energy, superconducting transition temperature.

## 1. Introduction

The unique properties of superconducting materials have found wide applications in both high and low electrical fields. Following the discoveries of cuprate and iron-based high-temperature superconductors [1-3], the exploration for novel high-temperature superconducting materials continues to intensify. Recent discussions have focused on intense debates concerning materials approaching room temperature superconductivity under strong high pressures [4-6], as well as the discovery of new nickel-based superconductors with  $T_c$  reaching over 80 degrees [7]. Theoretical and experimental studies have shown that microstructural variations in superconducting materials, such as ion heights, bond lengths, bond angles, interlayer distances, lattice matching, and pressure-induced microstructural changes, have an impact on the superconducting transition temperature [8-10]. Notably, in both cuprate and iron-based high-temperature superconductors, a block-layer model has been established based on the layer structure of superconductors, distinguishing between superconducting

and charge reservoir block layers [11, 12]. Investigating the interlayer combination energy and its relationship with the superconducting transition temperature  $T_c$  holds particular significance in understanding high-temperature superconductivity. Intergrowth-structured iron-based superconductors [13] are newly synthesized self-doped iron-based superconducting materials designed based on a summary of the structural characteristics and basic structure types of iron-based superconductors. They are characterized by intergrowth structures. Their composition must meet certain conditions, such as lattice matching between block layers, charge transfer between block layers, and ordered occupation of the same (or similar) crystal positions by ions in different block layers. In recent years, a series of intergrowth-structured iron-based superconductors have been reported, such as the  $AkAeFe_4As_4$  ( $Ak = K, Rb, Cs$ ) 1144 system formed by intergrowth of  $AkFe_2As_2$  and  $AeFe_2As_2$ , or the 12442 [14-18] system formed by intergrowth of  $AkFe_2As_2$  and 1111  $LnFeAsO$  systems. The space group of the 12442 system is  $I4/mmm$ .  $Ln$  and  $Ak$  ions have significantly different radii, alternatingly

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The interlayer combination energy ( $E_{\text{com}}$ ), the total combination energy of the cell ( $E_{\text{coh}}$ ), the combination energy of the superconducting block ( $E_{\text{pe}}$ ), and the combination energy of the charge reservoir block ( $E_{\text{re}}$ ) have been defined.

### 3. Experimental Results

#### 3.1 Crystal Combination Energy

Utilizing the established model and described computational methods, the crystal and interlayer combination energies of the 12442 system were calculated and analyzed. They were then compared with the superconducting transition temperature,  $T_c$ , as depicted in Fig. 2.

Fig. 2 illustrates the negative relationship between  $T_c$  and the interlayer combination energy in the  $\text{AkCa}_2\text{Fe}_4\text{As}_4\text{F}_2$  ( $\text{Ak} = \text{K, Rb, Cs}$ ) subclass of iron-based superconductors, where an increase in interlayer combination energy correlates with a decrease in  $T_c$ .

#### 3.2 Electronic Structure

In this paper, the calculations reveal that the antiferromagnetic state is more stable, albeit with minimal impact on energy. Building upon this, band structures and DOSs (density of states) under the antiferromagnetic state were computed. In Figs. 3-5a, band analysis indicates that for the superconducting

materials  $\text{AkCa}_2\text{Fe}_4\text{As}_4\text{F}_2$  ( $\text{Ak} = \text{K, Rb, Cs}$ ), eight bands intersect the Fermi surface along the paths  $\Gamma$ -X-M- $\Gamma$ -Z-R-A-Z, all exhibiting dense cylindrical hole-like pockets at the M and  $\Gamma$  points. Near the Fermi surface at the M point, there are eight electron pockets, while at the  $\Gamma$  point, there are eight hole-like pockets.

From the projected band structure in Figs. 3-5a, it is evident that the  $dz^2$  orbital of Fe exhibits the most crossings with the Fermi surface, occurring at  $\Gamma$ -X, M- $\Gamma$ , and Z-R. Consequently, among the five orbital bands, the  $dz^2$  orbital exerts the most significant influence on its properties. In general, the band structures of the five suborbitals of Fe 3d in the eight superconductors share three prominent features:

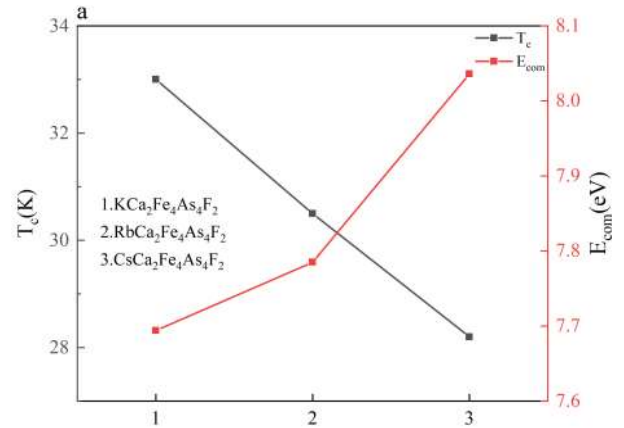


Fig. 2 Combination energy between blocks of 12442 intergrowth structures' relationship with  $T_c$ .

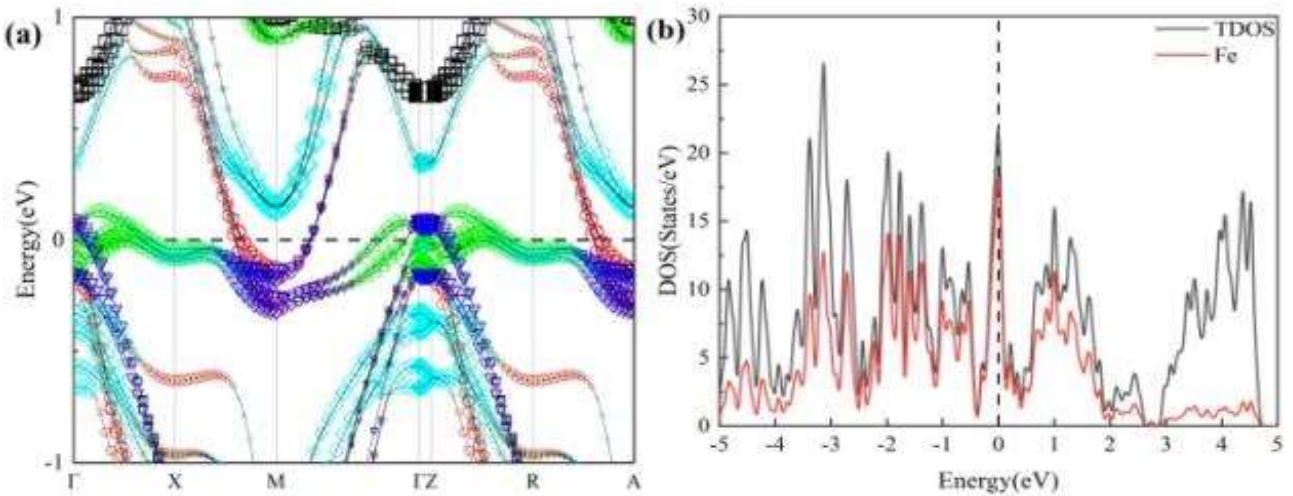
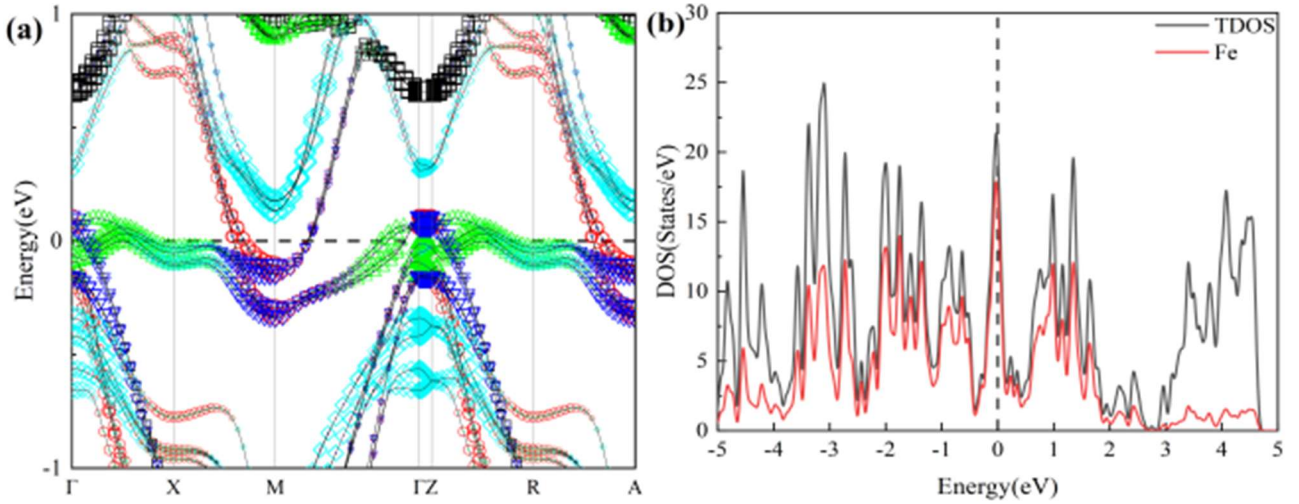
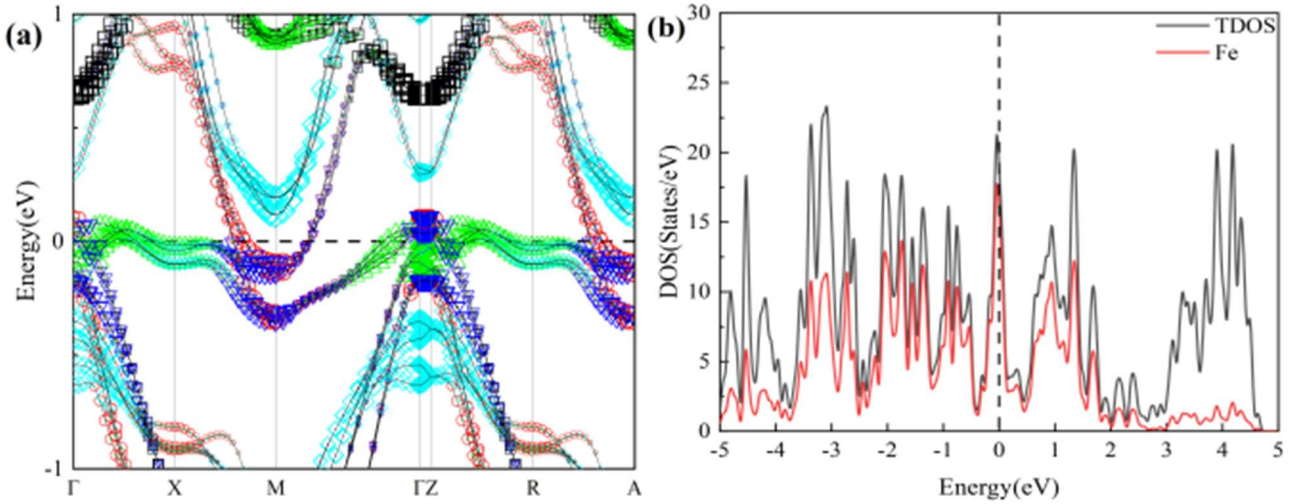


Fig. 3 DOS and fine band structure of Fe 3d of  $\text{KCa}_2\text{Fe}_4\text{As}_4\text{F}_2$ .



**Fig. 4** DOS and fine band structure of Fe 3d of  $\text{RbCa}_2\text{Fe}_4\text{As}_4\text{F}_2$ .



**Fig. 5** DOS and fine band structure of Fe 3d of  $\text{CsCa}_2\text{Fe}_4\text{As}_4\text{F}_2$ .

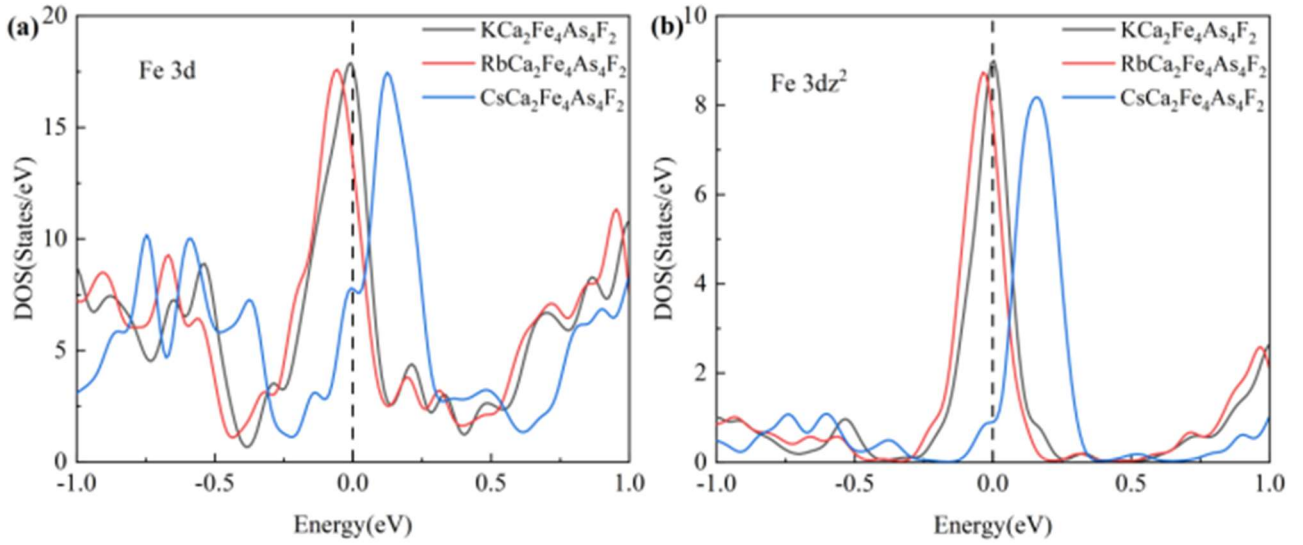
(1) Along the  $\Gamma$ -Z path, flat bands are observed, with the  $dx_z$ ,  $dy_z$ , and  $dz^2$  orbitals particularly evident. Notably, the  $dz^2$  orbital exhibits eight small flat segments near the Fermi surface from 0.05 to 0.1 eV and -0.2 to -0.15 eV, which are closely associated with superconductivity in iron-based superconductors and warrant attention.

(2) The  $dz^2$  orbital is the closest to the Fermi surface and crosses it most frequently, exerting a significant influence on  $T_c$ .

(3) Along the X-M path, several suborbitals intersect near the Fermi surface from -0.2 to -0.1 eV. It is evident that among the five suborbitals of Fe 3d, those contributing the most to the Fermi surface and having

a stronger impact on  $T_c$  are the  $dx_z$ ,  $dy_z$ , and  $dz^2$  orbitals of Fe. Particularly, the  $dz^2$  orbital has the most significant influence on the Fermi surface of 12442 materials, reflecting the coupling between layers along the z-direction and interlayer charge transfer, which correlates with the superconducting transition temperature. Therefore, the interlayer interaction energy calculated based on the block-layer model is correlated with  $T_c$ , providing a sound explanation from the electronic structure of the crystal.

Figs. 3-5b show the DOSs for 12442, from which it is observed that the Fermi surface exhibits the largest contribution from Fe. For ease of comparing the electronic structures among different materials,



**Fig. 6** Comparison of DOSs of Fe 3d and  $dz^2$  in  $AkCa_2Fe_4As_4F_2$  ( $Ak = K, Rb, Cs$ ) system.

Figs. 6a and 6b respectively present the DOS comparison of Fe's 3d orbitals and  $dz^2$  orbitals in the  $AkCa_2Fe_4As_2F_2$  and 12442 systems. From Fig. 6a, it is observed that there are distinctions in the DOS contributions of Fe's 3d orbitals among the  $AkCa_2Fe_4As_2F_2$  superconductors. Specifically, the DOS peak of  $KCa_2Fe_4As_2F_2$  is larger and closer to the Fermi surface compared to others. While the DOS peak positions of  $RbCa_2Fe_4As_2F_2$  and  $CsCa_2Fe_4As_2F_2$  are closer to  $KCa_2Fe_4As_2F_2$ , they gradually decrease in peak height and move further from the Fermi surface, resulting in electron numbers near the Fermi surface satisfying  $KCa_2Fe_4As_2F_2 > RbCa_2Fe_4As_2F_2 > CsCa_2Fe_4As_2F_2$ . This relationship aligns with our previous speculation, suggesting that interlayer interactions between the two blocks influence charge transport. Considering the formula relating the Fermi surface DOSs ( $N(E_F)$ ) to  $T_c$  in the BCS (Bardeen-Cooper-Schrieffer) theory, it is evident that  $N(E_F)$  and  $T_c$  in the 12442 system do not adhere to this relationship, indicating that 12442 superconductors do not conform to conventional superconductors according to the BCS theory. Considering our qualitative exploration of the relationship between interlayer combination energy and  $T_c$  through electronic band interpretation, Fe's  $3dz^2$  orbital better reflects the interaction between block

layers along the z-direction. Therefore, we primarily compare the influence of the  $dz^2$  DOSs among the five superconducting materials. In summary, for the 12442 layer iron-based superconducting structures, through comparative analysis of band structures and DOSs of each element, it is evident that Fe's 3d orbital electrons exert a decisive influence on the Fermi surface and superconducting properties. Furthermore, through detailed analysis of the fine bands and DOSs of Fe's five suborbitals, it is revealed that electrons in Fe's  $dz^2$  suborbital play a crucial role in the Fermi surface and superconducting properties, reflecting the coupling between block layers along the z-direction and interlayer charge transfer, which correlates with the superconducting transition temperature. The presence of interlayer combination energy affects charge transfer, thus the interlayer interaction energy calculated based on the block-layer model correlates with  $T_c$ , providing a sound explanation from the electronic structure of the crystal.

#### 4. Conclusions

This paper systematically investigates the interlayer combination energy, band structure, and DOSs of the 12442 layer iron-based superconducting systems  $AkCa_2Fe_4As_4F_2$  ( $Ak = K, Rb, Cs$ ) through theoretical

calculations. The following conclusions are drawn: Following the block-layer model of copper-based and iron-based superconductors, it is observed that in the 12442 layer iron-based superconductors  $\text{AkCa}_2\text{Fe}_4\text{As}_4\text{F}_2$ , larger interlayer combination energies correspond to lower  $T_c$ , while smaller interlayer interactions lead to higher  $T_c$ , consistent with the conclusions for the 1144 systems. Fe's 3d orbitals predominantly contribute near the Fermi level, with the dxz, dyz, and dz<sup>2</sup> orbitals exhibiting the highest contributions among Fe's five orbitals. Among them, the dz<sup>2</sup> orbital plays a crucial role in interlayer charge transfer.

Based on these research findings, it is concluded in this chapter that the relationship between interlayer combination energy and  $T_c$  exists in the 12442 layer iron-based superconductors  $\text{AkCa}_2\text{Fe}_4\text{As}_4\text{F}_2$  similar to cuprate superconductors.

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