

# Optimization of Molar Thermal Capacity for Graphite and N<sub>2</sub>

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**Abstract:** When teaching *Physical Chemistry* by Atkins et al., the author realized that the empirical formula for the molar thermal capacity at constant pressure  $C_{p,m} = a + bT + \frac{c}{T^2}$  has optimum  $C_{p,m}$  for an obtained temperature. The optimum is obtained by taking the derivative  $\frac{dC_{p,m}}{dT} = 0$ .

**Key words:** The mole capacity at constant pressure and mole, optimization of the mole capacity and temperature.

## 1. Introduction

Recently during past two to three decades optimization work has been done for various equations including the figure of merits in chromatography [1].

In present work the empirical equation for thermal capacity [2], has been used to obtain the  $T_{opt}$ ,  $C_{p,m_{opt}}$  where  $\frac{dC_{p,m}}{dT} = 0$  the result is obtained for the optimum temperature and optimum thermal capacity.

## 2. Theory

$$C_{p,m} = a + bT + \frac{c}{T^2}$$

In *Physical Chemistry* by Atkins et al. [2]:

$$\begin{aligned}\frac{dC_{p,m}}{dT} &= b - 2CT^{-3} = 0 \\ b &= 2CT^{-3} \\ T &= \sqrt[3]{\frac{b}{2C}}\end{aligned}$$

$$T_{opt} = \sqrt[3]{\frac{4.77 \times 10^{-3}}{2 \times 8.54 \times 10^5}}$$

For the graphite,  $b$ ,  $c$  are obtained from the table as given in Ref. [2].

$$\begin{aligned}T_{opt} &= \sqrt[3]{\frac{17.08}{4.77} \times 10^8 \times 10^1 \times 10^1} \\ &= \sqrt[3]{\frac{17.08}{4.77} \times 10^3} = 717\end{aligned}$$

$$\begin{aligned}C_{p,m_{opt}}(712) &= 16.86 + 4.77 \times 10^{-3} \\ &\times 717 + \frac{8.54 \times 10^5}{(712)^2} \\ &= 16.86 + 3.4 + 1.68 = 21.94\end{aligned}$$

By similar procedure,  $C_{p,m_{opt}}$  and  $T_{opt}$  are obtained for  $CO_2$  and  $N_2$ . The curves  $T$ ,  $C_{p,m}$  obtained for  $CO_2$  and  $N_2$  and graphite (Figs. 1-3). The  $C_{p,m_{opt}}$  and  $T_{opt}$  are graphed in Fig. 4.

## 3. Conclusion

To our knowledge the formula for the thermal capacity has not been optimized. In present work this is done.

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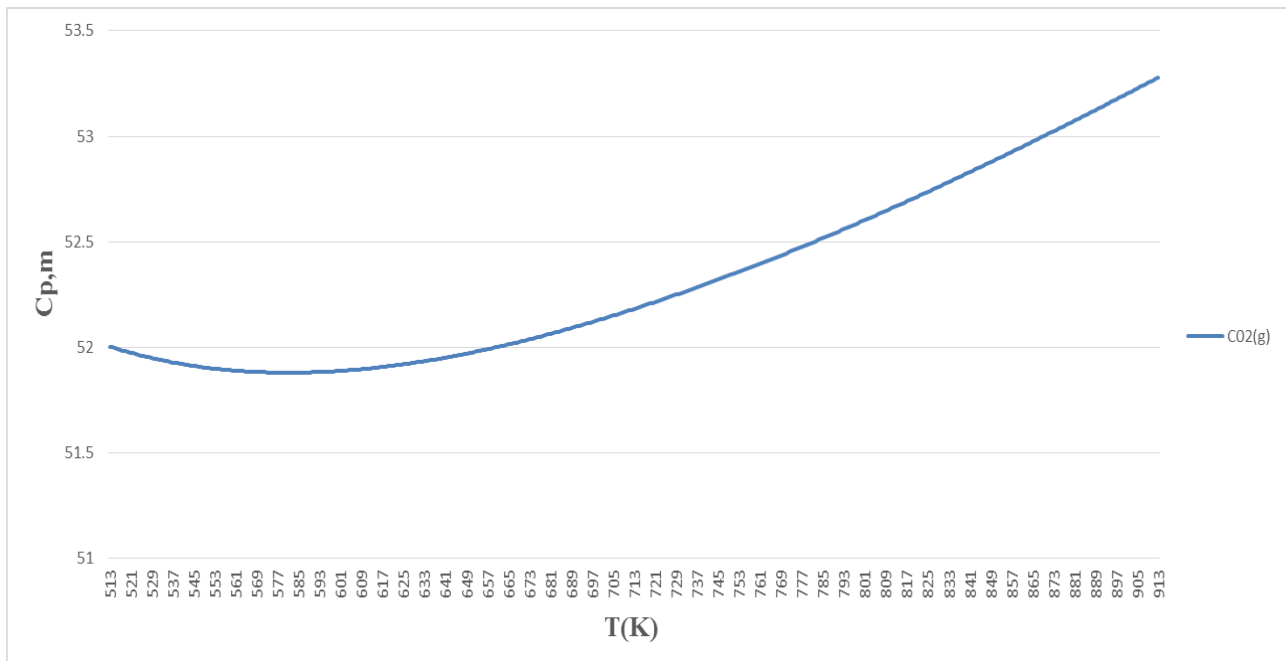


Fig. 1 Thermal capacity versus temperature for carbon dioxide.

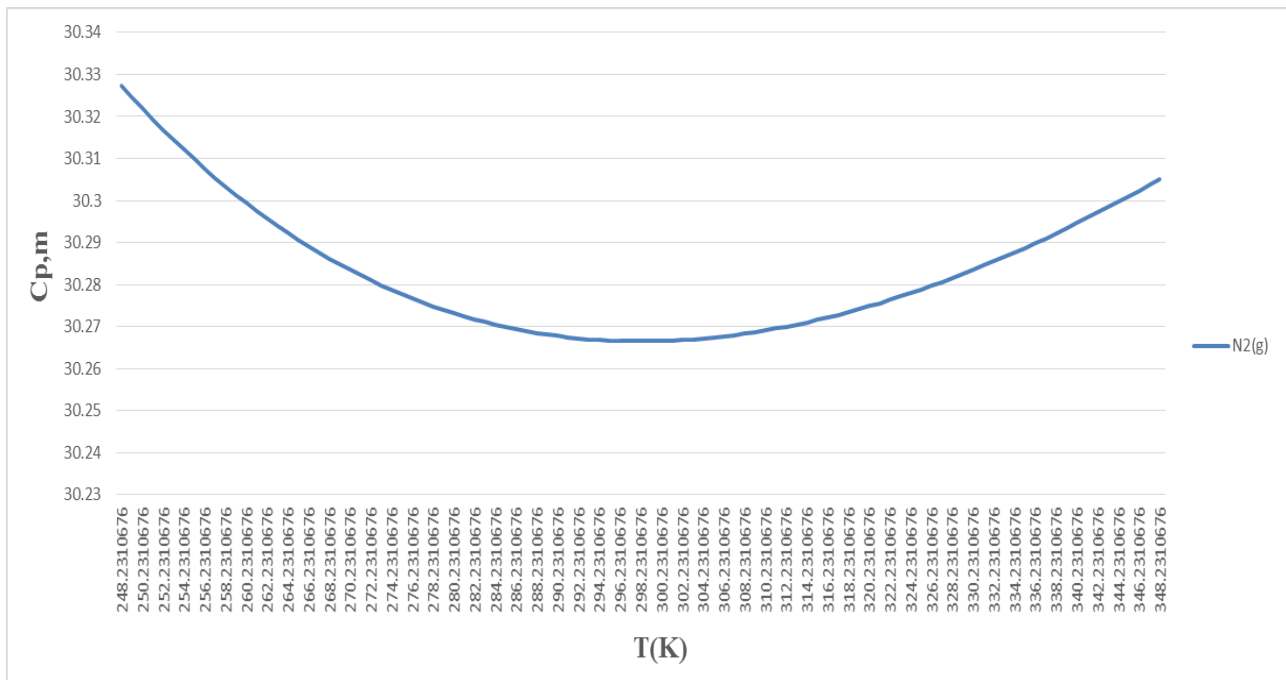


Fig. 2 Thermal capacity versus temperature for nitrogen.

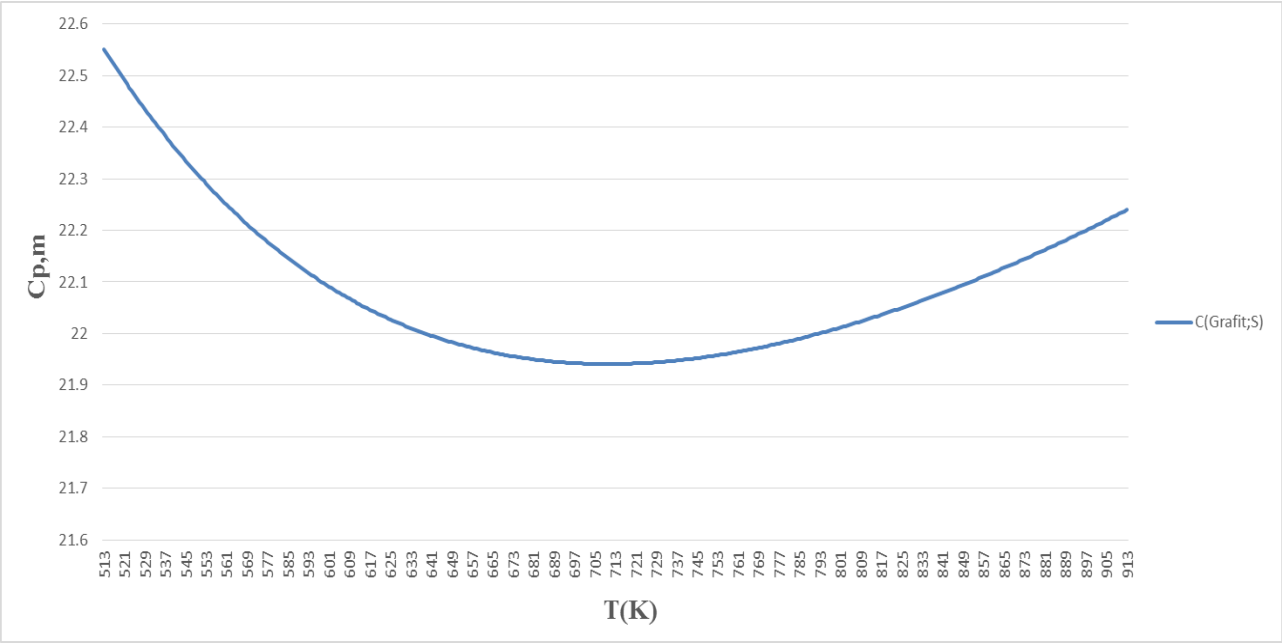


Fig. 3 Thermal capacity versus temperature for graphite.

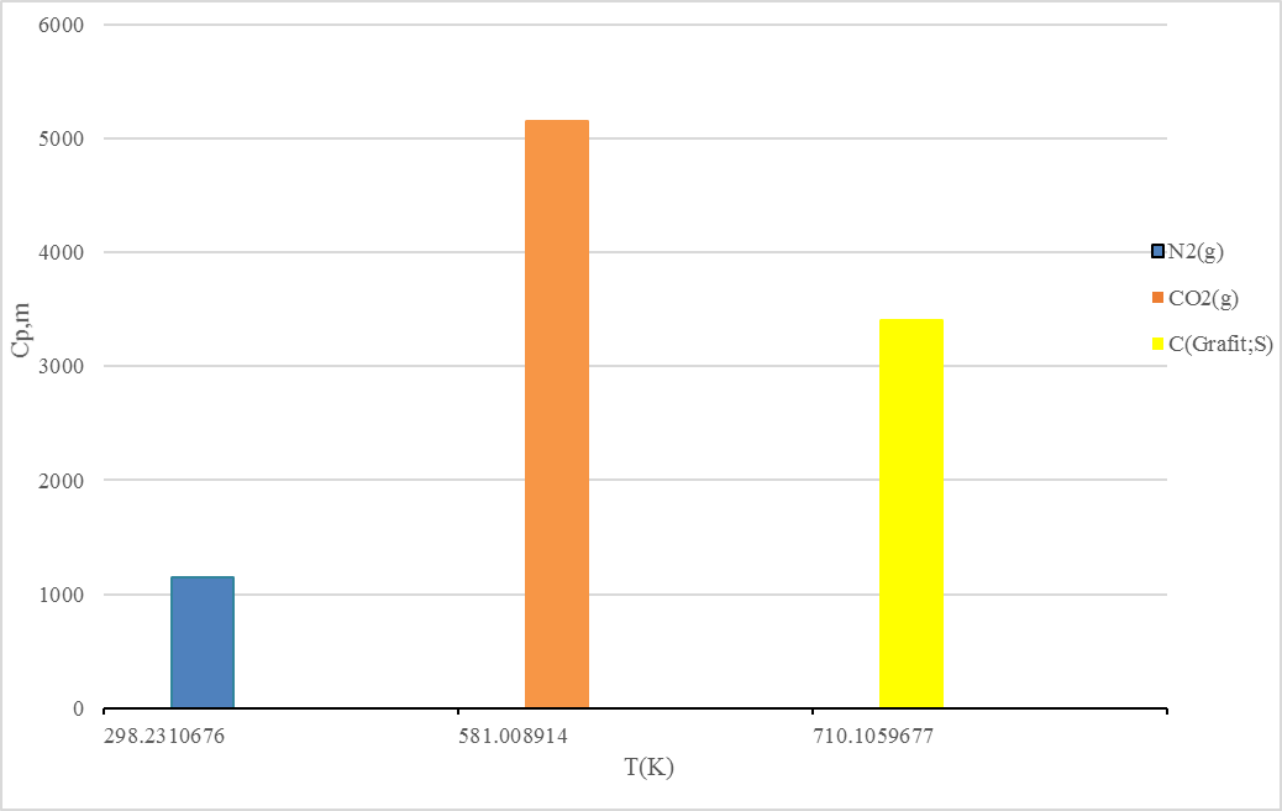


Fig. 4 Thermal capacity versus temperature optimization for three maters (nitrogen, carbon dioxide and graphite).

References

[1] Ghowsi, K. 1990. "Electrochemistry Insulator." Ph.D. dissertation, Louisiana State University.

[2] Atkins, P., et al. *Physical Chemistry*. 8th ed., translated by Parsafar, et al. Isfahan Technological University.