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Abstract: During last 45 years, two groups of the experimental data on critical heat flux were obtained in bare tubes, covering the pressures from atmosphere to near-critical point. One group of the data were obtained in the inner diameter of 2.32, 5.16, 8.05, 10.0 and 16.0 mm, respectively, with the ranges of pressure of 0.1-1.92 MPa, velocity of 1.47-23.3 m/s, local subcooling of 3.7-108.7 °C and heat flux of up to 38.3 MW/m². Another group of the data were obtained in the inner diameter of 4.62, 7.98 and 10.89 mm, respectively, with the ranges of pressure of 1.7-20.6 MPa, mass flux of 454-4,055 kg/(m²·s) and inlet subcooling of 53-361 °C. The results showed complicated effects of the pressure, mass flux, subcooling and diameter on the critical heat flux. They were formulated by two empirical correlations. A mechanistic model on the limit of heat transfer capability from the bubbly layer to the subcooled core was also proposed for all the results.

Key words: Critical heat flux, near-critical pressure, atmosphere, subcooled water.

Nomenclature

C_p	Specific heat at constant pressure, J/(kg·K)
D	Inner diameter, m or mm
DT	Subcooling, K
f	Friction factor
$f(\beta)$	Function of contact angle with surface
G	Mass flux, kg/(m ² ·s)
Н	Enthalpy, J/kg
ID	Inner diameter, mm
OD	Outer diameter, mm
L	Heated length, m
• m	Mass flow rate, kg/s
Р	Pressure, MPa
Pr	Prandtl number
q	Heat flux, W/m ²
q_{CHF}	Critical heat flux, MW/m ²
Re	Reynolds number
Q	Non-dimentional parameter, $Q = \frac{q}{\rho_l C_{pl} U_{\tau}}$
r	Radius, m

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Т	Temperature, K
у	Distance from the heated surface, m
y^+	Non-dimentional distance
U	Velocity, m/s
$\overline{U}_{\scriptscriptstyle B}$	Average velocity of bubbly layer, m/s
U_{τ}	Friction velocity, $\left(au_{_{W}} / ho_{_{l}} ight)^{0.5}$, m/s
$U^{\scriptscriptstyle +}$	Non-dimentional velocity, yU_{τ}/v_{l}
AVG	Average error
RMS	Standard error
σ	Surface tension, N/m
$\delta_{\scriptscriptstyle B}$	Thickness of bubbly layer, m
α	Void fraction
ε	Surface roughness, m
ho	Density, kg/m ³
$ au_w$	Wall shear stress, N
V	Kinematic viscosity, m ² /s
Subsc	ript
В	Bubble
С	Liquid core
с	Calculation
Е	Experiment

g Steam

- i Inlet
- l Liquid o Outlet
- s Saturation

1. Introduction

CHF (critical heat flux) is a major limit for the safety of nuclear reactors, because the occurrence of CHF could lead to a failure of fuel element [1-3]. During past six decades, the CHF has been investigated extensively over the world, and a variety of prediction methods have been proposed, including the empirical correlations, the physical models and the look-up tables [3-20]. Because of the extreme complexity of the phenomena and the lack of adequate knowledge of the mechanisms, all these predictive methods are heavily relied on the experimental data. For the CHF of near-critical pressures, which is interest for the SCWR (supercritical water-cooled reactors), only a limited experimental data have been published in Refs. [21-24].

In CIAE (China Institute of Atomic Energy), a great number of CHF experimental data of subcooled flow water were obtained at lower pressure to support the designs of research reactors, including the CHF in the rod bundle and the annuli heated from one-side or both-sides at steady-state or transient conditions [25-27]. They were the HWRR (heavy water research reactor), the HFR (high flux reactor) and the CARR (China advance research reactor), and were first put into operation in 1957, 1980 and 2011, respectively. During this period, the CHF experiments were also performed in the stainless-steel tubes of inner diameter of D = 2.32-16 mm at pressures less than 2 MPa [28, 29]. In recent years, the research was extended to the near critical pressure for the SCWR, and the experiments were performed in the Inconel-625 tubes of 4.62, 7.98 and 10.89 mm in diameter [30-32]. In the present investigation, the parametric trends were studied, and the empirical correlations were formulated. Based on all the subcooled experimental results, a mechanistic model on the limit of the

enthalpy of bubbly layer was proposed.

2. Experiment

2.1 Experimental Facilities and Test Sections

Two test facilities were used: (i) supercritical water test facility, and (ii) lower pressure test loop. In the former one, a three-head piston pump was applied to drive the de-ioned water through the dumping tank, the preheater, the test section, the heat exchanger and then to the water tank. The water flowed upward through the test sections. They were heated uniformly by a DC supply with capacity of 7,000 A \times 65 V. The preheater was heated by an AC supply. The experiments were performed by keeping the test power and the flow rate constants but increasing the preheater power slowly to approach the CHF condition. In the latter one, a centrifugal pump was applied to drive the de-ioned water. It flowed downward through the test sections. They were heated uniformly by a DC supply with capacity of 15,000 A \times 75 V. The experiments were performed by keeping the test power and flow rate constants but controlling the flow rate of the cooling water of heat exchanger to increase the water temperature slowly, until the CHF occurred. In all the experiments, the onset of CHF was detected by photocells [33]. Because the test section was heated uniformly the CHF always occurred near the end of heated length. The details of the experimental facility and the procedures were described in the previous papers.

For higher pressure, three test sections of Inconel-625 tubes were used: (i) 4.62 mm ID (inner diameter), 6.5 mm *OD* (outer diameter) and 0.5 m in heated length, (ii) 7.98 mm ID, 9.6 mm *OD* and 0.8 m in heated length, and (iii) 10.89 mm ID, 12.7 mm *OD* and 1.1 m in heated length. For lower pressure, five test sections of stainless-steel tubes were used. The inner diameters were: (i) 2.32 mm, (ii) 5.16 mm, (iii) 8.05 mm, (iv) 10.0 mm and (v) 16.0 mm. The details of geometries were listed in Table 2.

Major measurements of the parameters included: the outlet pressure, the flow rate, the inlet and outlet water temperatures of the test section, and the voltage and current across the heated tube. The readings were recorded by a data acquisition system or a multi-pen recorder (before 1980).

2.2 Experimental Results

2.2.1 Higher Pressure

The geometries and experimental conditions are listed in Table 1.

Fig. 1 shows the variations of critical heat flux, q_{CHF} , with inlet subcooling, DT_i , and local subcooling, DT_o , for different pressures. The q_{CHF} increases with the subcooling, DT_i or DT_o , increasing, and at higher pressure, the slope decreases. When the pressure exceeds 18 MPa, the variations of q_{CHF} with subcooling are weak, and the q_{CHF} is much lower than lower pressure due to the substantial decrease in the surface tension of the water. For a given high DT_o higher q_{CHF} corresponds to lower pressure, but at low DT_o lower q_{CHF} is obtained at rather low pressure.

The effect of mass flux on the CHF is shown in Fig. 2, indicating the q_{CHF} increase with the increase of mass flux for the same pressure. Fig. 3 shows the effect of

diameter on the CHF. For the nearly same pressure and mass flux, higher heat flux is obtained in smaller diameter. This effect is also observed by the other investigations, but the factor D^n is different with the exponent *n* from -0.1 to -0.5 [3].

An empirical formulation for the previous experiment of D = 7.98 mm was proposed as:

$$q_{CHF} = cq_s \tag{1}$$

where, q_s was the heat flux for the exit to reach the saturation temperature, evaluated by:

$$q_s = \frac{(H_s - H_i)GD}{4L}$$

where, H_i and H_s are the inlet enthalpy and saturation enthalpy, respectively, in J/kg, G is the mass flux in kg/(m²·s), D is the inner diameter and L is the heated length in m. In the present investigation, the factor c is modified to account for the three tubes as:

$$c = \operatorname{Min} \begin{bmatrix} 2.350(1 - 0.0307P) \\ (G(H_s - H_i))^{-0.35} (D / 0.008)^{-0.35}, 1.0 \end{bmatrix}$$
(2)

where, P is the pressure in MPa.

 Table 1
 The geometries and experimental conditions for higher pressures.

-	-					
D/L (mm/m)	P (MPa)	G (kg/(m ² ·s))	<i>DT</i> _{<i>i</i>} (K)	DT _o (K)	q_{CHF} (MW/m ²)	Number of data
4.62/0.5	1.8-20.6	556-4,055	110-354	1-169	0.77-9.3	118
7.98/0.8	2.0-20.4	476-1,653	53-361	3-158	0.26-4.95	193
10.89/1.1	1.7-20.0	454-1,144	169-345	4-141	0.92-3.3	74



Fig. 1 Variations of CHF with inlet and local subcooling for different pressures.



Fig. 2 The effect of inlet subcooling on the CHF for different mass fluxes (cal.-mechanistic model).



Fig. 3 The effect of diameter on the CHF (cal.—mechanistic model).



Fig. 4 Comparison of the experimental data with calculations of Eqs. (1) and (2) for higher pressures.

The comparison between the calculations by this correlation and the experimental data is shown in Fig. 4. The deviations of more than 90% of the data points are less than 10%, and the average error, AVG, and the standard error, RMS, are -0.43% and 6.0%, respectively.

2.2.2 Lower Pressure

For the experimental data of D = 2.32, 5.16, 8.05, 10.0 and 16.0 mm, the experimental conditions cover the ranges of pressures of 0.1-1.92 MPa, local subcoolings of 3.7-108.7 °C, velocities of 1.47-23.3 m/s and critical heat flux of up to 38.3 MW/m². The geometries and the conditions are listed in Table 2.

It is recognized that, for subcooled critical heat flux with L > 200 mm and $DT_o > 30$ K, the effect of heated length on the CHF disappears [8, 28, 29]. For the tube of D = 2.32 mm, the heated length is smaller, but the ratio of L/D exceeds 40. Therefore, the effect of heated length for these five tubes is negligible.

The effects of local subcooling, mass flux, pressure and diameter on the CHF are shown in Figs. 5-7. The CHF increases with the *G* and DT_o increasing. This is similar with the finding of other investigations. Because of the differences in the geometries and experimental conditions, these effects are different greatly in literature, and thus the results can not be compared at the extended conditions [4-10].

Table 2 The geometries and experimental conditions for lower pressures.								
No.	Diameter D (mm)	Heated length L (m)	Pressure P (MPa)	Velocity V (m/s)	Subcooling ΔT_o (K)	q_{CHF} (MW/m ²)	Number of data	
1	2.32	0.098	0.10-1.68	4.35-23.3	3.7-100.9	11.6-38.3	112	
2	5.16	0.255	0.13-1.78	2.59-22.3	6.2-89.6	8.4-29.3	63	
3	8.05	0.383, 0.396	0.14-1.92	1.88-15.9	8.3-88.2	4.7-17.9	65	
4	10.0	0.295, 0.400	0.15-1.66	3.39-9.26	30.3-89.5	4.4-10.9	53	
5	16.0	0.295, 0.390	0.19-1.29	1.47-13.4	36.7-108.7	4.2-14.6	56	

 Table 2
 The geometries and experimental conditions for lower pressures.



Fig. 5 The effects of local subcooling and mass flux on the CHF (cal.—mechanistic model).



Fig. 6 The effect of pressure on the CHF (cal.—mechanistic model).



Fig. 7 The effect of diameter on the CHF (cal.—mechanistic model).

An empirical correlation is proposed for the experimental data of $DT_o > 35$ K, as:

$$q_{CHF} = 0.108(1+0.104V)$$

$$(15P + DT_o^{1-0.1P})(\frac{D}{0.008})^{-0.35}$$
(3)

where, the critical heat flux q_{CHF} is in MW/m², velocity *V* in m/s, pressure *P* in MPa, local subcooling DT_o in K and inner diameter *D* in m. As can be seen, the velocity and local subcooling have strong effects on the CHF, and the diameter has a negative effect with the exponent n = -0.35. At lower pressure with $DT_o < 35$ K, the trend of CHF with DT_o appears weaker than larger subcooling due to larger bubble size and great pressure drop, and thus the results are not included in the present correlation [27].



Fig. 8 Comparison of the experimental results with the calculations of Eq. (3) for lower pressures.

The comparison between the calculations of Eq. (3) and the experimental data is shown in Fig. 8. For D = 2.32, 5.16, 8.05, 10.0 and 16.0 mm, the *AVG* is +1.28%, -4.87%, -1.08%, +4.41% and +1.08%, and the *RMS* is 10.77, 8.10, 7.97, 7.19 and 6.79%, respectively. The total *AVG* is +0.29% and *RMS* is 8.6%.

3. Mechanistic Model

For subcooled flow boiling CHF, two types of physical models have been proposed: (i) the critical enthalpy models for bubbly layer [12-14], and (ii) the liquid sublayer dryout model for a thin liquid layer beneath an intermittent vapor blanket [15-17]. The first model is applied in subcooled or low saturated condition, and the latter in high subcooling condition. In the present investigation, the model is similar to the first one. At high subcooling, the thickness of bubbly layer is determinant, and it is evaluated by the diameter of single bubble detached from the surface, multiplying a constant. For extending this model to lower subcooling condition, the thickness of bubbly layer is modified to account for the bubble crowding. The reader refers to the previous paper for details [30]. The major equations of the present model are represented in this paragraph. The schematic diagram of transport between the bubbly layer and the subcooled liquid core is shown in Fig. 9.



Fig. 9 Schematic diagram of transport between the bubbly layer and subcooled liquid core.

The thickness of bubbly layer is as:

$$\delta_{B} = k_{1} D_{B} (1 + k_{2} e^{-k_{3} P r Q})$$
(4)

where, the factor k_1 , k_2 and k_3 are constants as, $k_1 = 0.75$, $k_2 = 1,000$, and $k_3 = 1.0$. The *Pr* is the Prandtl number, Q is a parameter group (see Eq. (14)). D_B is the bubble or vapor blanket equivalent diameter, evaluated by [16]:

$$D_{B} = \frac{32\sigma f(\beta)\rho_{l}}{fG^{2}}$$
(5)

where, the σ is the surface tension in N/m, ρ_l is the liquid density in kg/m³ and G is the mass flux in kg/(m²·s). The $f(\beta)$ is a function relative to the contact angle with surface. In the previous study, it is represented as:

 $f(\beta) = 0.03$ for $P \le 10$ MPa

and

 $f(\beta) = 0.03(1 - 0.055(P - 10))$ for P > 10 MPa where, P is the pressure in MPa.

In the present investigation, for D = 2.32 mm, it is modified as:

$$f(\beta) = 0.03(1+1.5/D)$$
 for $D < 3.0$ mm (6)

The friction factor, f, is calculated by Colebrook-White equation combined with Levy's rough surface model [34], as:

$$\frac{1}{\sqrt{f}} = 1.14 - 2.0\log(\frac{\varepsilon}{D} + \frac{9.35}{Re\sqrt{f}})$$
(7)

where, *D* is the tube diameter, *Re* is the Reynolds number, and ε is the surface roughness, accounted by $\varepsilon = 0.75D_B$.

The velocity distribution in the liquid core is represented by Karman's universal law, as in Celata's model [16]:

$$U^+ = y^+ \qquad 0 \le y^+ < 5$$
 (8)

$$U^{+} = 5.0 \ln y^{+} - 3.05 \qquad 5 \le y^{+} < 30 \qquad (9)$$

$$U^{+} = 2.5 \ln y^{+} + 5.5 \qquad y^{+} \ge 30 \qquad (10)$$

The temperature distribution in the liquid core is as follows [35]:

$$T_0 - T = QPry^+ \qquad 0 \le y^+ < 5$$
 (11)

$$T_{0} - T = 5Q \left\{ Pr + \ln \left[1 + Pr(\frac{y^{+}}{5} - 1) \right] \right\}$$

$$5 \le y^{+} < 30$$
(12)

$$T_0 - T = 5Q \left[Pr + \ln(1 + 5Pr) + 0.5 \ln(\frac{y^+}{30}) \right]$$
$$y^+ \ge 30$$
(13)

with

$$Q = \frac{q}{\rho_l C_{pl} U_{\tau}} \tag{14}$$

The Eqs. (8)-(13) are assumed valid in the region of

 $\delta_B \leq y \leq r$, and the T_0 is a referent value, determined by $T = T_s$ at $y = \delta_B$.

From the heat balance equation, the local enthalpy *H* is calculated by:

$$H = H_i + \frac{4qL}{GD}$$

and

$$H \overset{\bullet}{m} = H_{C} (\overset{\bullet}{m} - \overset{\bullet}{m}_{B,g} - \overset{\bullet}{m}_{B,l}) + H_{g} \overset{\bullet}{m}_{B,g} + H_{l} \overset{\bullet}{m}_{B,l}$$
(15)

where, *m* is the total flow rate, $m_{B,g}$ and $m_{B,l}$ are the vapor and liquid flow rate in the bubbly layer, respectively, H_g and H_l are the vapor and liquid enthalpy, and H_C is the enthalpy of liquid core, calculated from the average temperature T_C , as:

$$T_{C} = \frac{\int_{\delta_{B}}^{r} TU(r-y) dy}{\int_{\delta_{B}}^{r} U(r-y) dy}$$

where, the r is the radius of tube.

The m, $m_{B,g}$ and $m_{B,l}$ are evaluated by:

$$m = \pi D^2 G / 4$$

•
$$m_{B,g} = \pi (D - \delta_B) \delta_B \alpha_B \rho_g \overline{U_B}$$

and

•
$$m_{B,l} = \pi (D - \delta_B) \delta_B (1 - \alpha_B) \rho_l \overline{U_B}$$

where, α_B is the void fraction in the bubbly layer. It is taken as $\alpha_B = 0.9$. The $\overline{U_B}$ is the average velocity of bubbly layer, estimated by:

$$\overline{U_B} = 0.5U_{y=\delta}$$

Calculation is started with a test heat flux q ($\leq q_s$), and the CHF is obtained through an iterative process. At low subcooling, the q_c is close to the q_s , and not sensitive to δ_B , thus the maximum value of δ_B is simply set as 0.1*D*.

The calculations of this mechanistic model are also compared with the experimental results in Figs. 2, 3, 5-7. In Fig. 10, the calculations are compared with the experiment for higher pressures. The *AVG* is -1.2%, -0.12% and +1.4%, and the *RMS* is 5.37%, 4.86% and 6.86% for the diameter of 4.62, 7.98 and 10.89 mm, respectively. The total data are calculated with *AVG* of -0.16% and *RMS* of 5.45%.

For lower pressure with smaller diameter D = 2.32 mm, the results are underestimated with the original model by about 11%. Then, the function of contact angle is modified to the Eq. (6), and the results are improved properly. Fig. 11 shows the comparison of the calculations of this model with the experimental results for lower pressure. For all the 334 data points with $DT_o > 35$ K, the *AVG* is +1.75%, -4.13%, +2.23%, +5.81% and +5.12%, and the *RMS* is 7.33%, 7.47%, 5.28%, 7.24% and 8.52% for D = 2.32, 5.16, 8.05, 10.0 and 16.0 mm, respectively. The total data are calculated with *AVG* of +2.1% and *RMS* of 7.2%.

4. Comparison with the Calculations of 95 CHF Look-up Table

The 86 CHF-Look-up table was used in the reactor safety analysis code RELAP5/MOD3.3. The effect of diameter was accounted by a factor $(D/8)^n$ with the *n*



Fig. 10 Comparison of the calculations of mechanistic model with the experimental data for higher pressures.



Fig. 11 Comparison of the calculations of the mechanistic model with the experimental results for P < 2 MPa.

ranged from -0.1 to -0.5 [36]. This look-up table was modified in 1995 [20]. The present experimental results are compared to the 95-CHF Look-up table in Fig. 12. At the normal operation condition of the PWRs (pressurized water cooled reactors) with P = 15.4 MPa and G = 3,994 kg/(m²·s), the experimental results of D = 4.62 mm are close to the calculations by 95-LUT(1) with n = -0.35, but are a little lower than 95-LUT(0) with n = -0.5. For the research reactors with P = 0.71 MPa and G = 7,800 kg/(m²·s), the experimental results $q_{CHF, E}$, with D = 8.05 mm are also close to the $q_{CHF, c}$. At the conditions of P = 8.65 MPa and G = 1,630 kg/(m²·s), which could occur at the accident condition of PWRs, the results of D = 7.98 mm are also close to the 95-LUT for $X_o < -0.04$, but some deviations of about 20% are observed at $X_o = -0.02$. At the conditions of P = 20 MPa, and G = 1,600 kg/(m²·s), which are similar to the normal operation conditions of the supercritical water-cooled reactors, the results $q_{CHF, E}$ of D = 7.98 mm are lower than the $q_{CHF, c}$ by about 30%-40%.



Fig. 12 Comparison of the present experimental results with the calculations of 95-Look-up table for different conditions (95-LUT(0) by n = -0.5, 95-LUT(1) by n = -0.35).

5. Conclusions

The subcooled flow boiling CHF experiment is conducted in bare tubes of D = 2.32-16 mm, covering the pressures ranging from atmosphere to near-critical point and wide ranges of flow conditions. The parametric trends are studied systematically. The experimental results are formulated by two empirical correlations and are validated by a mechanistic model. Major conclusions are achieved as follows:

• The CHF increases as mass flux and subcooling increasing. At higher pressure, the slope of q_{CHF} with subcooling decreases. When the pressure tends toward

the critical point the CHF decreases rapidly.

• For the same local conditions, higher CHF is attained in smaller diameter of tube, as accounted by $D^{-0.35}$ for the present conditions.

• For the present conditions, the critical heat flux is formulated by two empirical correlations for lower pressures and higher pressures, respectively.

• The mechanistic model, based on the limit of bubbly layer enthalpy, can predict the CHF for the whole range of conditions.

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